# Sai Sivakumar

Email: sivakumars@ufl.edu University of Florida

#### Goals

Pursuing a B.Sc. in Mathematics, minors in Computer Science and Physics. Intending to complete a Ph.D. in Mathematics.

## Education

- 2020- B.Sc. in Mathematics, University of Florida, 3.98 GPA
- 2020- Minor in Computer Science, University of Florida, 4.0 GPA
- 2020- Minor in Physics, University of Florida, 4.0 GPA
- 2016–2020 IB Diploma, Stanton College Preparatory High School, 4.0 GPA

### Research

#### Summer 2023 REU at the University of Minnesota, Twin Cities, Two projects:

- Worked with Dr. Christine Berkesch and four undergraduates on a project in algebraic geometry and homological algebra. We extended results in previous work by Harada et al. to provide two methods for finding virtual resolutions (Berkesch et al.) for ideals of sets of points in P<sup>n</sup> × P<sup>m</sup>, and created this report (preprint in progress).
- 2) Worked with Dr. Michael Perlman and four undergraduates on a project in commutative algebra, homological algebra, and representation theory. We studied GL<sub>n</sub>(k)-stable ideals of polynomial rings in positive characteristics and their free resolutions. We provide a method for finding minimal free resolutions for a wide class of GL<sub>2</sub>(k)-stable ideals generated in a single degree in any positive characteristic. We created this report (preprint in progress).

#### Summer 2022 REU at the Georgia Institute of Technology

Worked with Dr. Ashley Wheeler and two other undergraduates on a project in algebraic geometry. We studied the toric varieties given by the vanishing of principal 2-minor ideals in affine and projective space. We proved a number of properties about these varieties, and created this poster.

## Talks and Presentations

- Oct. 2023 Virtual resolutions of points in  $\mathbb{P}^n \times \mathbb{P}^m$ To the UF Algebra seminar; outlining the first project I worked on at the UMN Twin Cities mathematics REU.
- Sep. 2023 Stable ideals and their syzygies Talk for undergraduates about the second project I worked on at the UMN Twin Cities mathematics REU.
- Apr., Jul. Fourier analysis on LCA groups and Pontryagin duality
  - 2023 For Dr. Sin's MAS7397 Introduction to representation theory class and for the Student Summer Representation Theory Seminar at the University of Minnesota, Twin Cities (abstract and recording).
- Oct. 2022 What is representation theory? Intro to the topic for undergraduates, applications in Fourier analysis.

May 2022	The Smith normal form
	For a summer course in topological data analysis; discussed the Smith normal form for Euclidean domains and PIDs and applications in computing simplicial homology.
Feb.–Mar.	Fourier analysis on finite Abelian groups
2022	Five lectures briefly outlining the theory and applications as they appear in Stein and Shakarchi I.
Feb. 2022	Combinatorial proof of existence of Sylow subgroups
	To the UF Algebra seminar; proof due to Wielandt in 1959.
Oct. 2021	The Hamilton quaternions
	With classmate; discussed history, properties, functions of quaternionic variables, applications.
Falls	Annual LATEX seminar
2021–2023	Joint with the UF Graduate Mathematics Association (GMA) and the UF Association for Women in Mathematics (AWM) chapter.
Jun. 2021	The inverse Laplace transform
	Integral definition of the inverse Laplace transform, computations using the integral using the residue theorem. (YouTube; gave an abridged version of this talk Jan. 2023.)
Mar. 2021	The fundamental theorem of calculus
	Proved the theorem at a high school/pre-real analysis level.

## Skills

LATEX 4+ years

Macaulay2 used in both REUs I attended

Java, C++ with understanding of data structures and algorithms

# Outreach and Service

- Aug. 2023– President of the University Math Society at UF. I manage the club (delegating responsibilities, reserving venues, responding to queries, etc.), ensure all events run smoothly, form collaborations with the AWM chapter and the GMA, and encourage a friendly, inclusive environment for all members.
- Aug. 2021- Teaching assistant and grader for MAP2302 Elementary Differential Equations.
- Mar. 2021– Moderator for a large online community exceeding 160,000 members globally, which seeks to stimulate mathematical discussion and interest, as well as to provide assistance with math.

Aug. Academic Director of the University Math Society at UF. I scheduled talks from

- 2021–May professors, gave talks myself, and encouraged undergraduate students to give talks. 2023
- Aug.-Dec. Contributed around 47 pages to the solution manual for *Concepts in Calculus III* by 2020 Miklos Bona and Sergei Shabanov, working with two other students to form 141 pages of solutions which are posted on the course page.

# Honors and Awards

2023 The Kermit Sigmon Scholarship.\$200, awarded every spring to promising undergraduate mathematics majors (info).

2020-2023	Dean's list.
	Fall 2020, Spring 2021, Summer 2021, Fall 2021, Spring 2022, Fall 2022, Spring 2023.

	Graduate Mathematics Coursework	
Course codes in the 4000s indicate mixed undergraduate-graduate courses.		
No code	Modular Forms, <i>Fall 2023</i> , (reading course)	
	With Dr. Jeremy Booher, reading from Ch. 7 of A Course In Arithmetic by Serre and from A First Course in Modular Forms by Diamond and Shurman. In preparation for senior thesis.	
MAT6932	Analytic Number Theory, <i>Fall 2023</i> , (audited)	
	Topics in analytic number theory including proving the prime number theorem, sieve methods, probablistic number theory. Professor's notes.	
MTG6256	Differential Geometry 1, <i>Fall 2023</i> , (audited)	
	Basic concepts of differential and Riemannian geometry. Using do Carmo.	
MAP6505	Mathematical Methods for Physics and Engineering I, Fall 2023	
	Topics in real analysis, complex analysis, geometry which are used in physics and engineering. Theory of distributions, distributional solutions to linear differential equations, and Green's functions. Professor's notes.	
MAS7397	Introduction to Representation Theory, Spring 2023	
	Module-theoretic representation and character theory of finite groups and of finite- dimensional semisimple complex Lie algebras, theorems of Burnside and Frobenius. Profes- sor's lectures following content from Fulton-Harris.	
MTG6347	Topology II, Spring 2023	
	Singular, axiomatic, and cellular homology/cohomology, and their algebraic structure and dualities. Professor's notes and chapters 10-12, parts of chapters 16-18 in tom Dieck.	
MAA6407	Complex Analysis II, Spring 2023	
	Weierstrass factorization, analytic continuation and Riemann zeta function, harmonic functions, Picard theorems, and other topics. Professor's notes and chapters 7, 9, 10, parts of 12 in Conway.	
MAA6617	Analysis II, Spring 2023	
	Introductory functional analysis. Theory of Banach and Hilbert spaces, linear operators, $L^p$ spaces and their duality, $L^1$ and $L^2$ Fourier transform, theory of distributions. Touched on Banach algebras. Professor's notes.	
MAS6332	Algebra II, Spring 2023	
	Projective, injective, and flat modules. Introduction to homological algebra, group cohomology, category theory, commutative algebra, and algebraic geometry. Chapters 15-17 in Dummit and Foote and professor's notes.	
MAT6932	Calculus of Variations and Optimal Control, Fall 2022	
	Covered basic theory of calculus of variations and optimal control following several examples. Professor's lectures.	
MTG6346	Topology I, <i>Fall 2022</i>	
	Topology I – Covered the fundamental group, covering spaces, intro homotopy theory, cofibrations and fibrations, homotopy groups, CW complexes, singular homology. Chapters 1-6, 8, 9 of tom Dieck.	
MAA6406	Complex Analysis I, Fall 2022	
	Analytic functions, integral formulas, zeroes and singularities of functions, Morera's and Goursat's theorems, Cauchy's theorem and integral formula, Laurent series, spaces of holomorphic functions. Professor's notes and chapters 1-7 in Conway.	

MAA6616	Analysis I, <i>Fall 2022</i>
	Sigma-algebras, measures, the Lebesgue measure, signed measures, integration of measurable functions, modes of convergence, and differentiation theorems. Professor's notes.
MAS6331	Algebra I, Fall 2022
	Field and Galois theory, as well as tensor products and some coverage of projective modules. Chapters 10.4, 10.5, 13, 14 of Dummit and Foote.
MTG4303	Introductory Topology II, Spring 2022
	Basic algebraic topology and topics from point-set topology. Chapters 5-6, 9-12 from Munkres.
MAP4341	Introduction to Partial Differential Equations, Spring 2022
	Elementary theory of solving partial differential equations. Professor's notes and lectures.
MAS5312	Introduction to Algebra II, Spring 2022
	Rings, fields, modules. Chapters 7-13 of Dummit and Foote.
MAA5228	Modern Analysis I, <i>Fall 2021</i> , (audited)
	Metric spaces and topology, convergence of sequences and series, continuity, differentiation. Chapters 1-5 of Rudin PMA.
MAS5311	Introduction to Algebra I, Fall 2021
	Group theory. Chapters 1-6 from Dummit and Foote.